

1. Write as a product of linear factors. A zero is provided. Then, Sketch the following polynomials on the axis provided.

1)  $f(x) = -x^4 + x^3 + 2x^2$   ~~$x = -1$~~

Zeros  
 $x = 0, 0, -1, 2$

$$x^2(-x^2 + x + 2)$$

$$f(x) = x^2(x+1)(x-2)$$

$$\begin{array}{r|rrrr} -1 & -1 & 1 & 2 & \\ & & 1 & -2 & \\ \hline & -1 & 2 & 0 & \end{array}$$

$$-x + 2 = 0$$

$$x = 2$$

2)  $g(x) = x^3 + 5x^2 + 2x - 8$   $x = -2$

$$g(x) = x^3 + 5x^2 + 2x - 8 \quad \text{Zero } x = -2$$

$$\begin{array}{r|rrrr} -2 & 1 & 5 & 2 & -8 \\ & & -2 & -6 & 8 \\ \hline & 1 & 3 & -4 & 0 \end{array}$$

$$x^2 + 3x - 4 = 0$$

$$(x+4)(x-1)$$

$$x = -4 \quad x = 1$$

4)  $p(x) = -x^4 + 8x^3 + 3x^2 - 130x + 200$ , 5 is double root

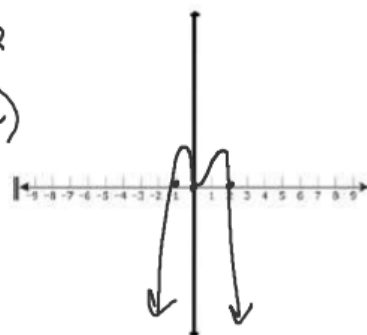
$$\begin{array}{r|rrrrrr} 5 & -1 & 8 & 3 & -130 & 200 & \\ & & -5 & 15 & 90 & -200 & \\ \hline 5 & -1 & 3 & 18 & -40 & 0 & \\ & & -5 & -10 & 40 & & \\ \hline & -1 & -2 & 8 & 0 & & \end{array}$$

$$-x^2 - 2x + 8 = 0$$

$$x^2 + 2x - 8 = 0$$

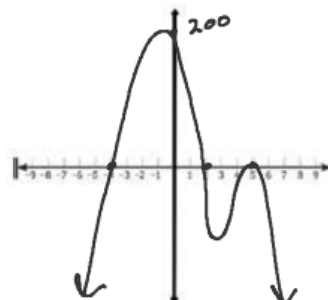
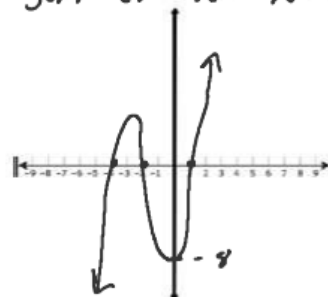
$$(x+4)(x-2)$$

$$x = -4 \quad x = 2$$



Zeros  $x = -2, -4, 1$

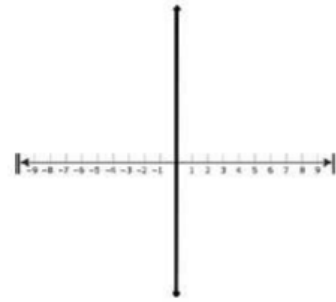
$$g(x) = (x+2)(x+4)(x-1)$$



Zeros  $x = 5, 5, -4, 2$

$$p(x) = (x-5)^2(x+4)(x-2)$$

5)  $j(x) = -2x^5 + 18x^4 - 5x^3 + 36x^2 + 5x - 54$ , 3 has multiplicity of 3



6)  $f(x) = 2x^4 - 6x^3 - 30x^2 + 38x + 60$ , 2 and 5 are zeros

$$\begin{array}{r|rrrrr}
 2 & 2 & -6 & -30 & 38 & 60 \\
 & & 4 & -4 & -68 & -60 \\
 \hline
 5 & 2 & -2 & -34 & -30 & 0 \\
 & & 10 & 40 & 30 & \\
 \hline
 & 2 & 8 & 6 & 0 & 
 \end{array}$$

$$2x^2 + 8x + 6 = 0$$

$$x^2 + 4x + 3 = 0$$

$$(x-3)(x+3)$$

6)  $f(x) = -x^5 + 6x^4 + x^3 - 54x^2 + 72x$ ,  $x^2 - 9$  is a factor

$$f(x) = x(-x^4 + 6x^3 + x^2 - 54x + 72)$$

$$\begin{array}{r|rrrrr}
 3 & -1 & 6 & 1 & -54 & 72 \\
 & & -3 & 9 & 30 & -72 \\
 \hline
 -3 & -1 & 3 & 10 & -24 & 0 \\
 & & 3 & -18 & 24 & \\
 \hline
 & -1 & 6 & -8 & 0 & 
 \end{array}$$

$$-x^2 + 6x - 8 = 0$$

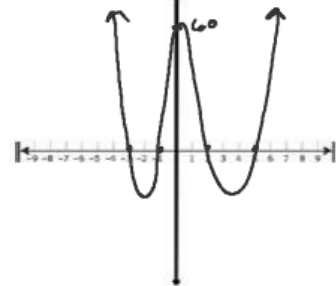
$$x^2 - 6x + 8 = 0$$

$$(x-4)(x-2) = 0$$

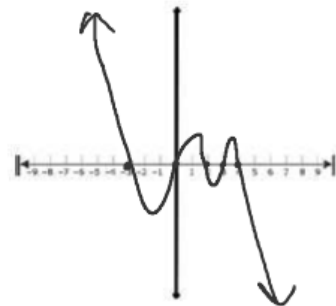
$$x = 4 \quad x = 2$$

Zeros: 2, 5, -3, -1

$$(x-2)(x-5)(x+3)(x+1)$$



Zeros:  $x = 3, -3, 0$



Zeros:  $x = 0, 3, -3, 4, 2$

$$x(x-3)(x+3)(x-4)(x-2)$$